

Exercises – Phylogenetics

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Exercise List 7 — 01.12.2015

Due to: 08.12.2015

Exercise 1 Additive metric, ultrametric.

(4 Points)

Given the following matrices:

i)	A	B	C	D	E
A	0	10	10	10	4
B		0	2	6	10
C			0	6	10
D				0	10
E					0

ii)	A	B	C	D	E
A	0	3	7	9	10
B		0	8	10	11
C			0	4	5
D				0	3
E					0

Decide for i) and ii) whether the matrix describes an additive or even an ultrametric metric. Explain your result.

Exercise 2 Properties of distances.

(4 Points)

For every distance function d applies the following relation:

$$“d \text{ is ultrametric}” \Rightarrow “d \text{ is additive}” \Rightarrow “d \text{ satisfies the triangle inequality}”$$

Prove this relation by showing the following items:

- (a) “ d satisfies the *three point condition*” \Rightarrow “ d satisfies the *four point condition*”

Proof sketch: Pick four arbitrary elements and proceed: Denote the two elements with the smallest distance as a and b . Denote the other two elements as c and d such that $d_{ac} \leq d_{ad}$. Now we can order a, b, c and d in two different, binary, ultrametric trees. **Which?** In both cases several three point conditions are fulfilled (**Which?**) that can be combined/transformed to the wanted four point condition. **How?** (The case where the distances don't correspond to a binary topology is not considered here. We cover this case by allowing edges of length 0. For example: $((a:2,b:2,c:2):1,d:3)$; would be the binary tree $((a:2,b:2):0,c:2):1,d:3)$;)

- (b) “ d satisfies the four point condition” \Rightarrow “ d satisfies the triangle inequality”

Hint: The four point condition can be used on three points aswell.

Exercise 3 Agglomerative clustering.

(4 Points)

Given the following distance matrix:

	A	B	C	D	E	F
A:	0	1	4	9	9	6
B:		0	2	9	9	4
C:			0	9	9	3
D:				0	5	6
E:					0	4
F:						0

Use the following methods to reconstruct phylogenetic trees from the matrix.

- (a) *Single linkage clustering.*
 (b) *WPGMA.*

State the corresponding matrix in every intermediate step. Write down the final tree in the end. If there are more possibilities, show all of them.

- (c) Compare the results and decide whether the matrix is ultrametric. Explain!