

Exercises – Phylogenetics

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<https://gi.cebitec.uni-bielefeld.de/Teaching/2016winter/Phylogenetik>

Exercise Sheet 11 — 24.01.2017

Due: 31.01.2017

Task 1 Evolutionary Markov Processes.

(3 points)

Use your own words to explain three of the five properties an *evolutionary Markov process (EMP)* has by definition. Write 2-5 sentences per property. Do not simply reproduce the formulas.

Task 2 Modeling of Sequence Evolution.

(7 points)

Consider the following model of nucleotide substitution:

$$\pi = \left(\frac{1}{4}, \frac{1}{4}, \frac{1}{4}, \frac{1}{4}\right)$$

$$Q = \begin{pmatrix} -5/8 & 3/8 & 1/8 & 1/8 \\ 3/8 & -5/8 & 1/8 & 1/8 \\ 1/8 & 1/8 & -5/8 & 3/8 \\ 1/8 & 1/8 & 3/8 & -5/8 \end{pmatrix}$$

$$P(t) = \begin{pmatrix} 1 - (x + 2y) & x & y & y \\ x & 1 - (x + 2y) & y & y \\ y & y & 1 - (x + 2y) & x \\ y & y & x & 1 - (x + 2y) \end{pmatrix}$$

where

$$x = \frac{1 - 2 \exp(-t) + \exp(-t/2)}{4}, \quad y = \frac{1 - \exp(-t/2)}{4}$$

- How much PEM is the model calibrated to?
- Recalibrate the corresponding matrix to 1 PEM.
(You are **not** supposed to calibrate **both** matrices to 1 PEM.)
- How much PAM is the model calibrated to?
- Recalibrate the corresponding matrix to 1 PAM.
(You are **not** supposed to calibrate **both** matrices to 1 PAM.)

Task 3 Jukes-Cantor Correction.

(5 points)

Consider an alignment with length 900 and 65 substitutions (no InDel included). We assume an evolution of the sequences following the Jukes-Cantor model.

- What is the Jukes-Cantor corrected distance d (in PEM) of the sequences?
- How many mutation events occurred approximately?
- How many mutation events occur and how many substitutions in the alignment would appear, if the distance d between the sequences is 20 PEM?