

Advanced Sequence Analysis
Summer 2019

Exercises

Number 1 (12.04.2019), Discussion: 26.04.2019

1. If they exist, find words
 - (a) of lengths 2, 4 and 10 that are primitive;
 - (b) of lengths 2 and 5 with a period of length 1;
 - (c) of lengths 5 and 10 whose only period is of length 4;
 - (d) of lengths 6 and 10 whose only periods are of lengths 3 and 5.
2. Compute the
 - (i) Hamming distance
 - (ii) subword distance
 - (iii) edit distance
 - (iv) prefix distancebetween the following pairs of words:
 - (a) aabbabaabababa and abbaabaabaabba,
 - (b) abababaaababab and abbbbaaabbab.
3. What is the worst case running time for the Naive String Matching algorithm discussed in class? Give an example where this running time is achieved. Present a more efficient algorithm that has optimal running time.
4. Modify the algorithm for computing the subword distance such that it computes the edit distance.
5. Develop a polynomial-time algorithm that finds the longest increasing subsequence in an array X of n numbers, $X[1, \dots, n]$.

Hint: Use dynamic programming using an auxiliary array L storing in $L[i]$ the length of the longest increasing subsequence of the prefix $X[1, \dots, i]$.